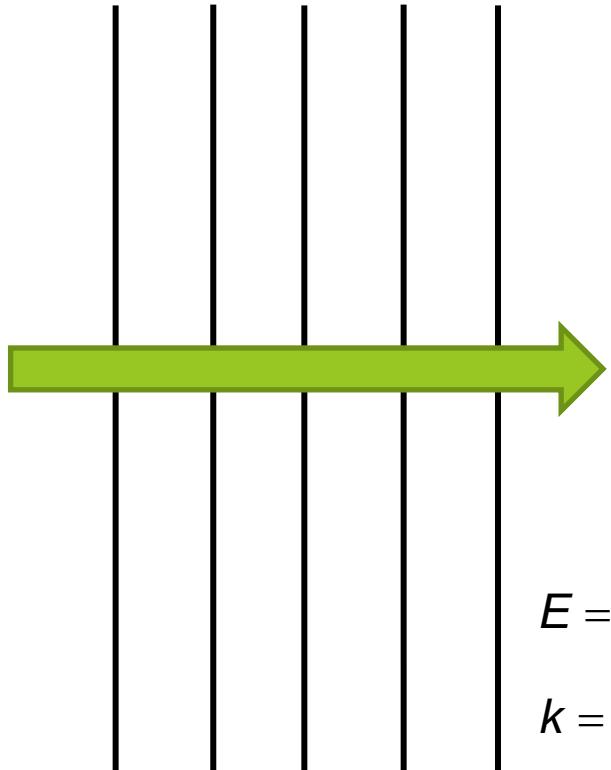
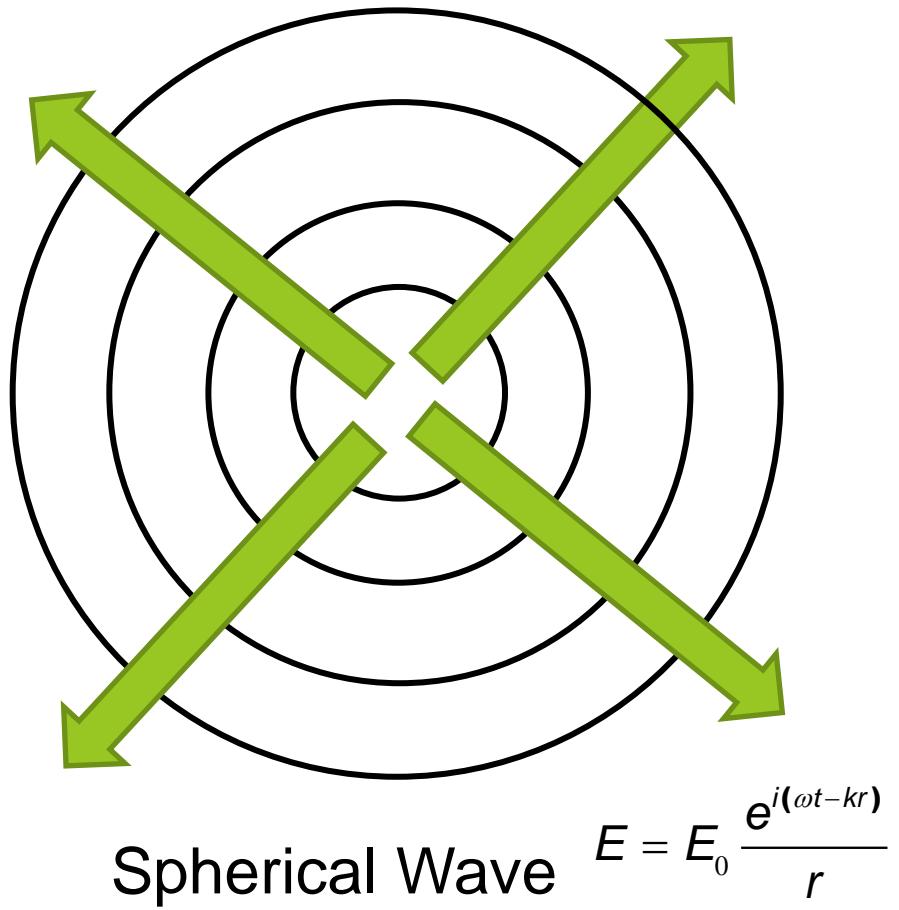


# Waves in Free Space



Plane Wave

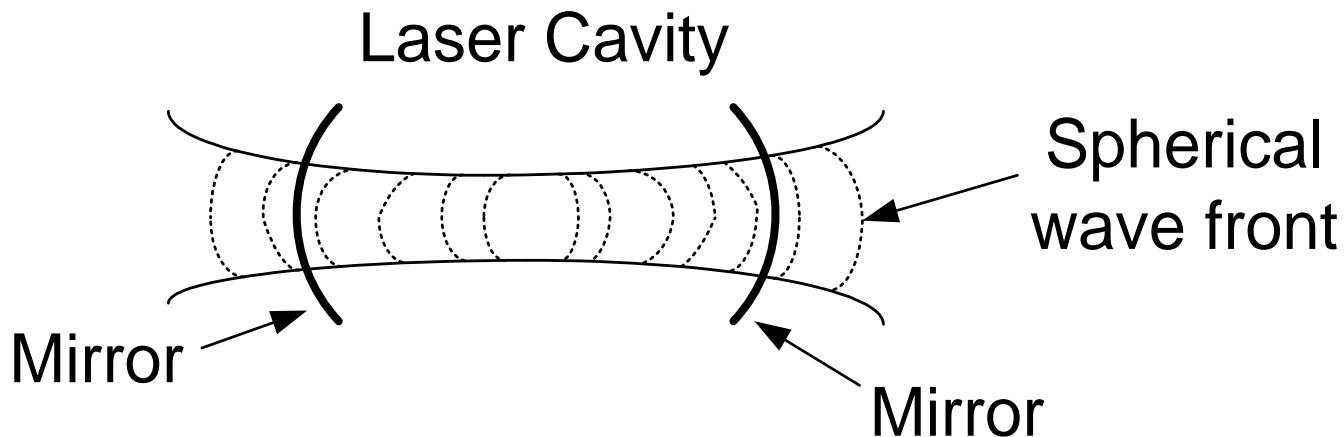
$$E = E_0 e^{i(\omega t - kz)}$$
$$k = \frac{2\pi}{\lambda_0} n$$



Spherical Wave

$$E = E_0 \frac{e^{i(\omega t - kr)}}{r}$$

# Gaussian Beams



$$E(r, z, t) = E_0 \frac{W_0}{W} e^{-r^2/W^2} e^{-jk(z + \frac{r^2}{2R})} e^{j\phi} e^{j\omega t}$$

$$w(z)^2 = w_0^2 \left[ 1 + \left( \frac{z}{z_R} \right)^2 \right]$$

Spot Size

$$R(z) = z \left[ 1 + \left( \frac{z_R}{z} \right)^2 \right]$$

Radius of Curvature

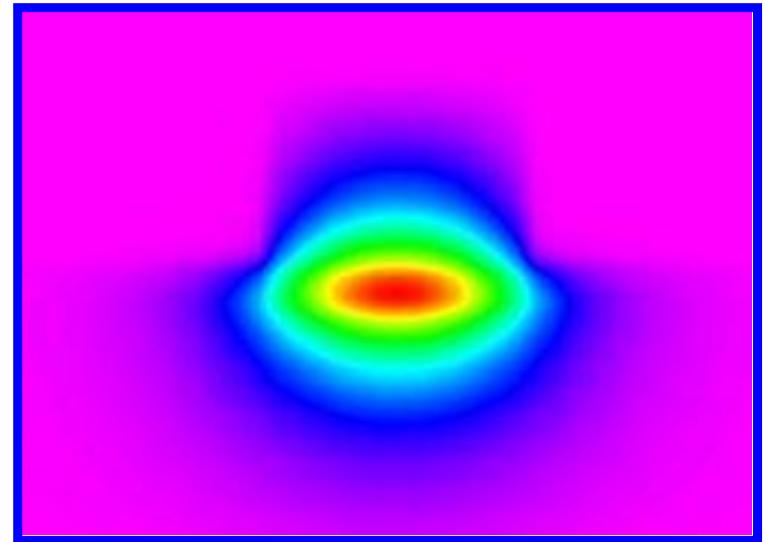
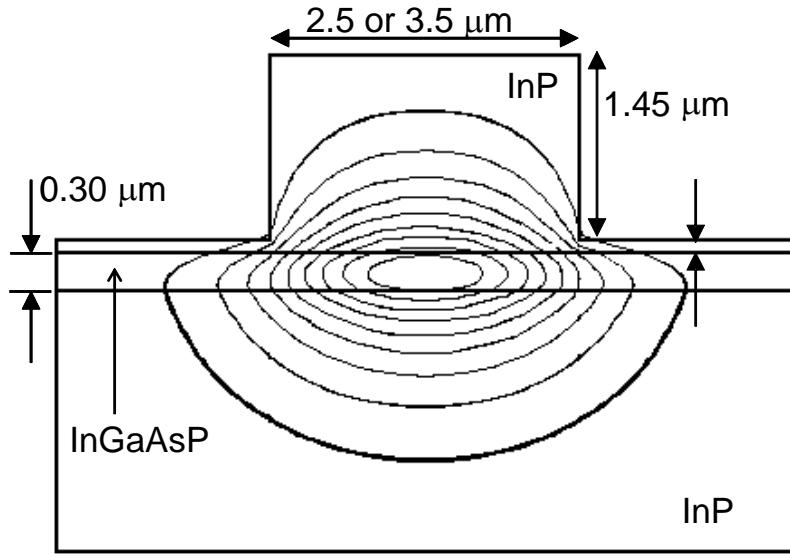
$$\phi(z) = \tan^{-1}(z/z_R)$$

Extra Phase Factor

$$z_R = \frac{\pi w_0^2}{\lambda}$$

Rayleigh Range

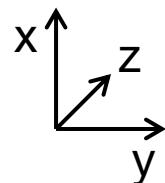
# Guided Waves



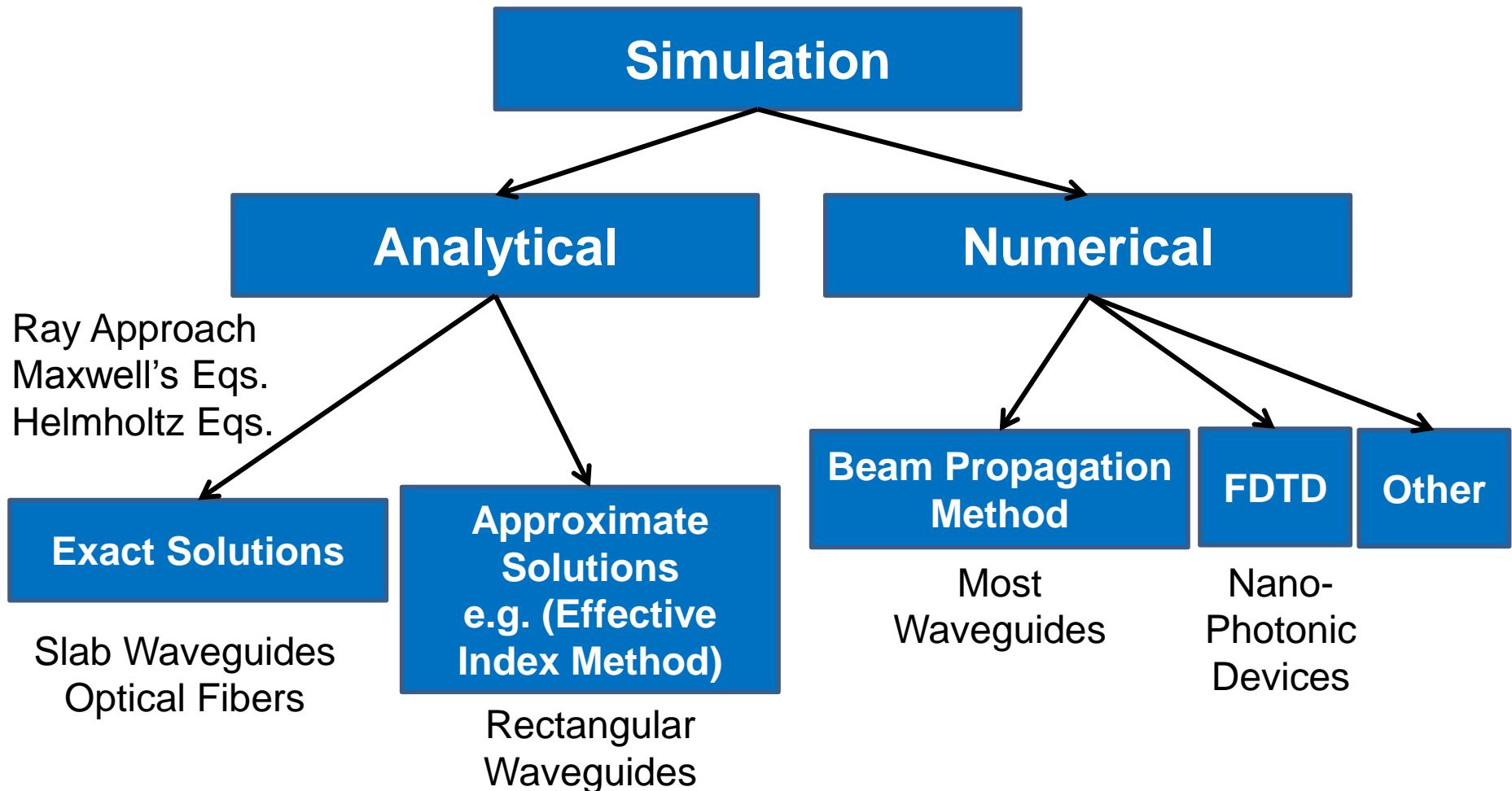
$$\vec{E}(x, y), \vec{H}(x, y)$$

$$\vec{E}(x, y), \vec{H}(x, y)$$

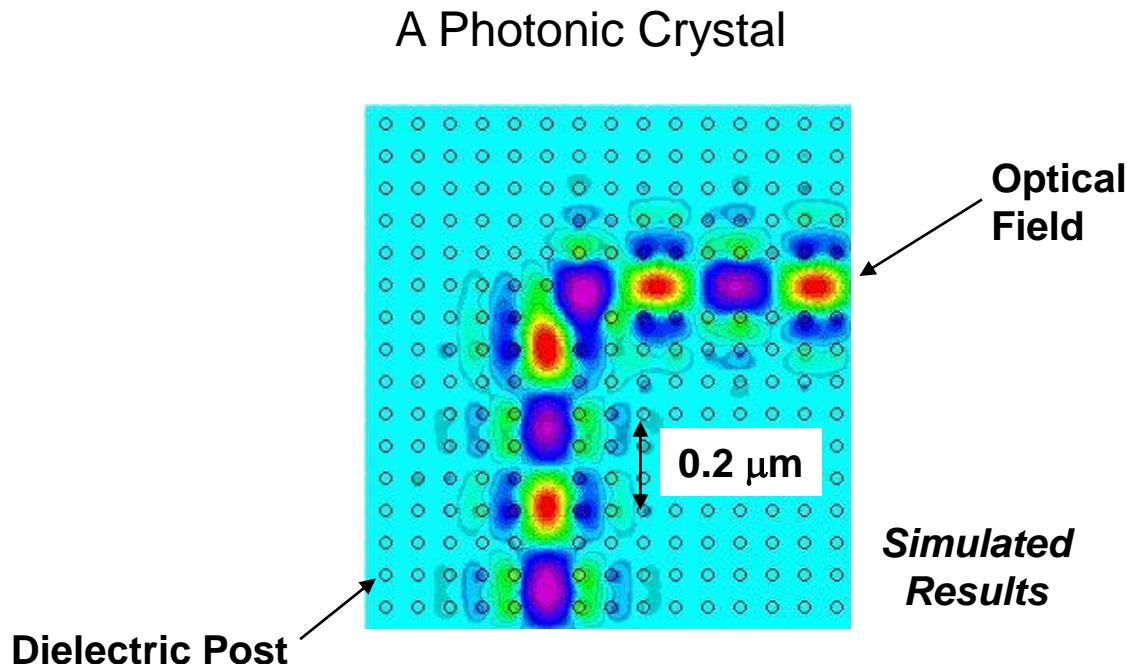
$$e^{i \frac{2\pi}{n_{\text{eff}}} z} = e^{i \beta z}$$



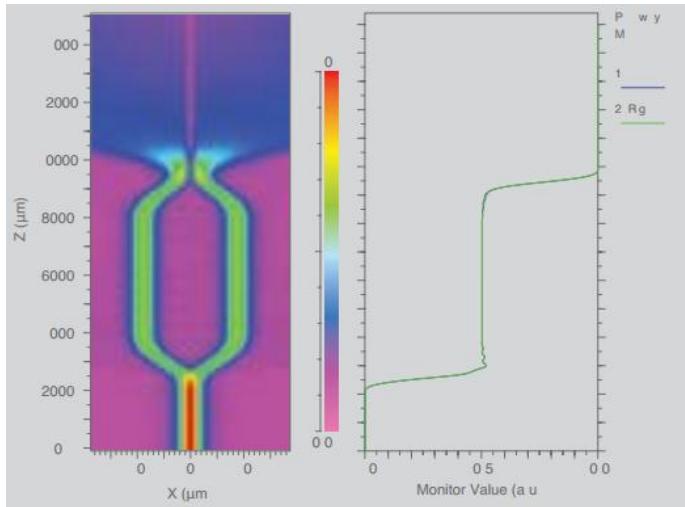
# Analysis of Guided Waves



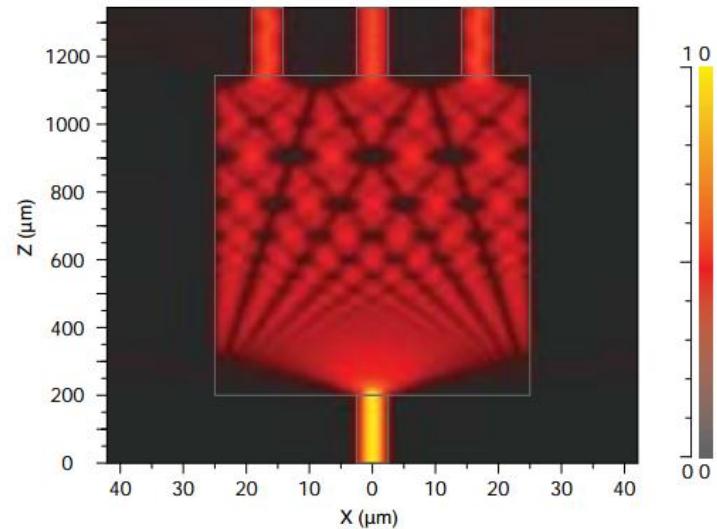
# An Simulation for Which FDTD is Particularly Well-Suited



# Beam Propagation Method



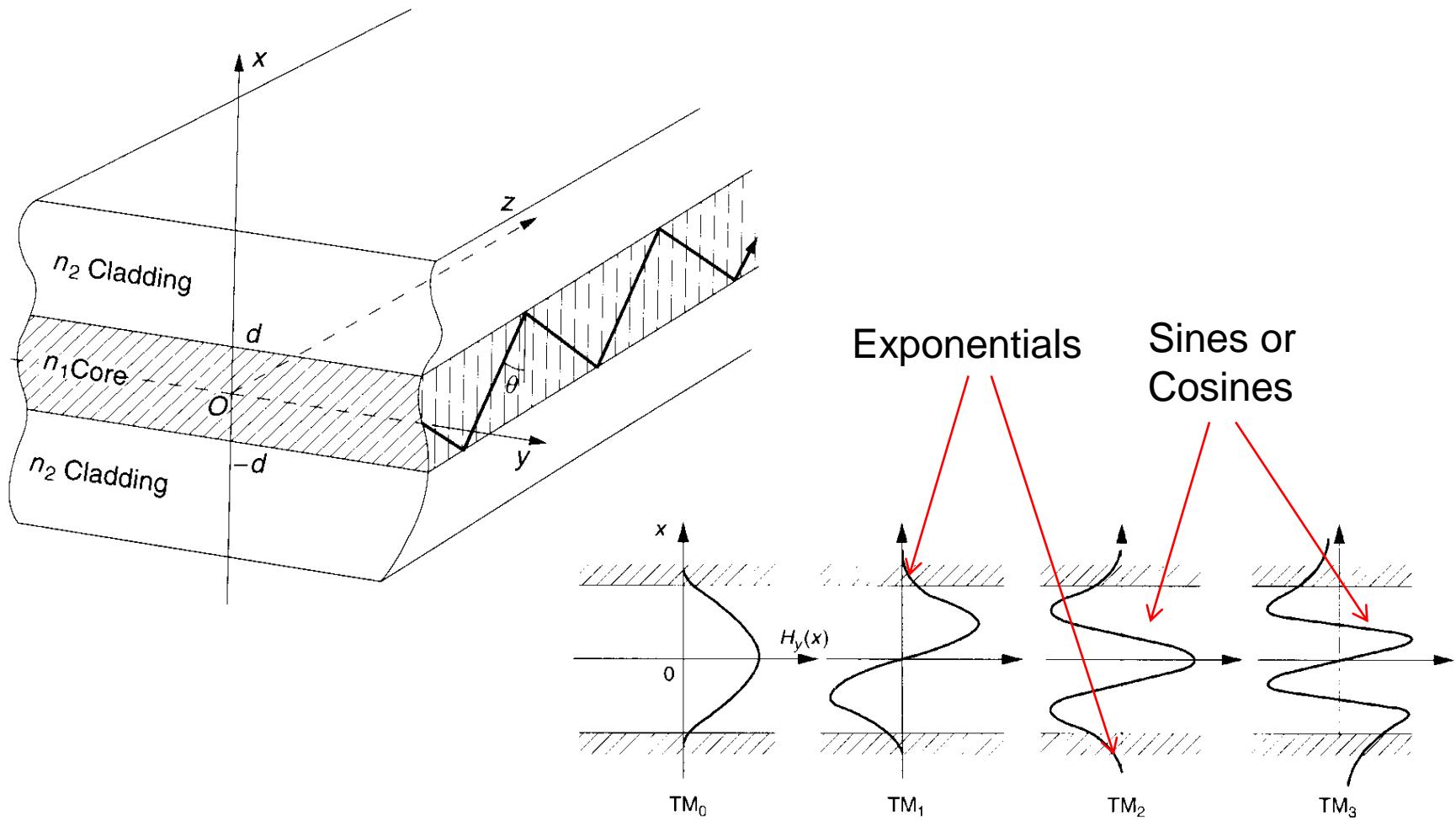
BeamPROP simulation of a Mach-Zehnder modulator operating completely out of phase. The power in each arm is shown on the right.



BeamPROP simulation of a multi-mode interference device (MMI) operating as a 1 to 3 optical splitter

- Approximate, but can be used to simulate waves in a wide variety of photonic devices.

# Slab Waveguides



**Figure 9.3** Distribution of the  $H_y$  field in the slab optical guide. The field distributions correspond to the modes in Fig. 9.2.

# Question

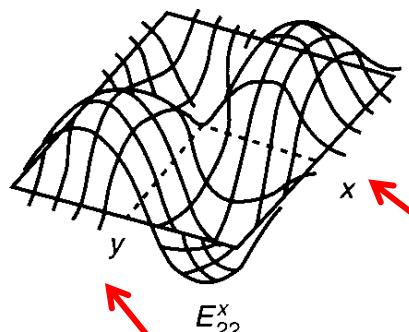
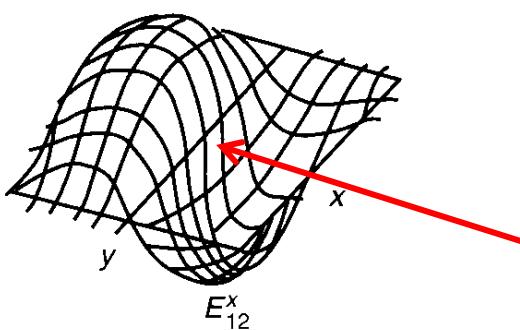
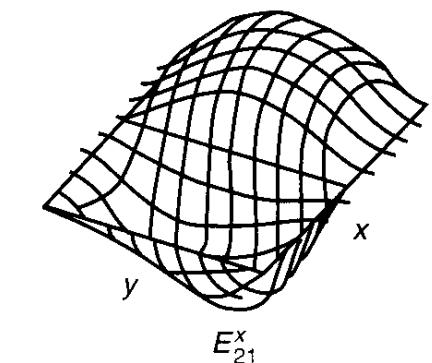
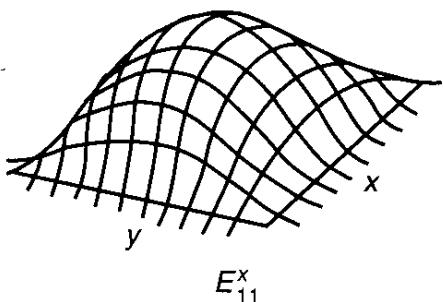
What functions could be used to describe the cross-sectional profile for a guided optical wave in waveguide with a rectangular cross-section?

High Refractive Index

Low Refractive Index

Send response to [akost@arizona.edu](mailto:akost@arizona.edu)

# Field Profiles in Rectangular Waveguides



Commonly used approximation

$$E(x, y) = E(x)E(y)$$

we use a sine or cosine function for  $E(x)$  and  $E(y)$  in the core (high index region) of the guide

We use an exponential function for  $E(y)$  out here

We use an exponential function for  $E(x)$  out here

# Question

What functions are used to describe the cross-sectional profiles for optical waves in optical fibers?

Hint: Optical fibers have cylindrical Symmetry

Send response to [akost@arizona.edu](mailto:akost@arizona.edu)

# Field Distributions in Optical Fibers

EH<sub>νμ</sub> Modes:

$$E_r \square -J_{\nu+1}(\kappa_{\nu\mu}r)\cos\nu\phi$$

$$E_\phi \square -J_{\nu+1}(\kappa_{\nu\mu}r)\sin\nu\phi$$

$$H_r \square J_{\nu+1}(\kappa_{\nu\mu}r)\sin\nu\phi$$

$$H_\phi \square -J_{\nu+1}(\kappa_{\nu\mu}r)\cos\nu\phi$$

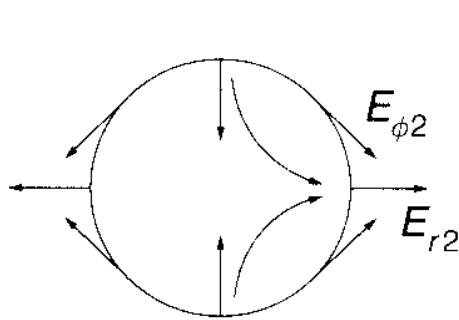
HE<sub>νμ</sub> Modes:

$$E_r \square J_{\nu-1}(\kappa_{\nu\mu}r)\cos\nu\phi$$

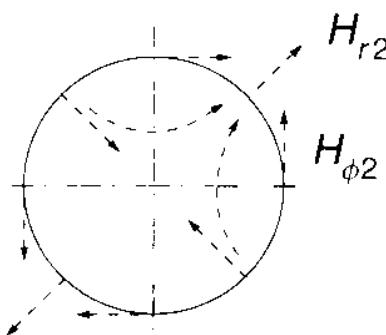
$$E_\phi \square -J_{\nu-1}(\kappa_{\nu\mu}r)\sin\nu\phi$$

$$H_r \square J_{\nu-1}(\kappa_{\nu\mu}r)\sin\nu\phi$$

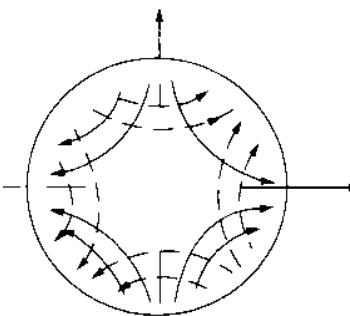
$$H_\phi \square J_{\nu-1}(\kappa_{\nu\mu}r)\cos\nu\phi$$



E<sub>2</sub> field



H<sub>2</sub> field



HE<sub>21</sub> mode